Jim Foster and Tamas Szabo* (szabot@uww.edu), 800 Main St, Dept. of Math. and Comp. Sci., UW Whitewater, Whitewater, WI 53190. Diameter graphs of polygons and the proof of a conjecture of Graham.
We show that for an $n$-gon with unit diameter to have maximum area, its diameter graph must contain a cycle, and we derive an isodiametric theorem for such $n$-gons in terms of the length of the cycle. We then apply this theorem to prove Graham's 1975 conjecture that the diameter graph of a maximal $2 m$-gon ( $m \geq 3$ ) must be a cycle of length $2 m-1$ with one additional edge attached to it. (Received September 13, 2007)

