Andrew Shallue* (ashallue@math.ucalgary.ca), University of Calgary, Department of Mathematics and Statistics, 2500 University Drive NW, Calgary, Alberta T2N1N4, Canada, and Eric Bach. Composites with large sets of strong liars. Preliminary report.
The Miller-Rabin primality test is often used in practice to determine if an integer is prime or composite. This test generates a random $a \in(Z /(n))^{*}$ and then determines whether $n$ is a strong pseudoprime to the base $a$. For composite $n$, the set $S(n)$ of $a$ for which the test mistakenly returns "prime" has size at most $(n-1) / 4$. Our goal is to find infinite classes of composite integers with large sets $S(n)$. For example, Carmichael numbers with three prime factors, all congruent to $1 \bmod 4$, have $S(n)=\phi(n) / 4$. However, it seems difficult to prove that infinitely many exist. In this talk we present "almost Carmichael" numbers, a provably infinite class, and give lower bounds on $|S(n)|$ when $n$ is almost Carmichael. (Received September 15, 2008)

