1046-11-311Adriana Julia Salerno* (asalerno@math.utexas.edu), 3202 Grooms St Apt G, Austin, TX
78705. Rational Points and Hypergeometric Functions.

We study the number of \mathbb{F}_q -rational points $N(\lambda)$ of a hypersurface in $P_{\mathbb{F}_q}^{n-1}$ defined by the equation

$$x_1^d + \dots + x_n^d = d\lambda x_1^{h_1} \cdots x_n^{h_n}$$

where $d|q-1, h_1 + \cdots + h_n = d$ and $g.c.d.(d, h_1, \ldots, h_n) = 1$. We find that $N(\lambda)$ is the finite field version of a hypergeometric function, and we explore the possibility that hypergeometric functions may always appear when counting points. (Received September 11, 2008)