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**Olivier Kwegna Heubo\*** (oheubo@nmsu.edu), New Mexico State university, Department of Mathematical sciences, Las Cruces, NM 88003-8001. *Kronecker function rings of transcendental field extensions.*

We consider an extension  $F/D$  where  $F$  is a field and  $D$  a subring of  $F$ , we denote by  $\Sigma(F/D)$  the set of all valuation rings  $V$  such that  $D \subseteq V \subseteq F$  and  $V$  has quotient field  $F$ . We study the rings on the form  $\bigcap_{V \in \Sigma(F/D)} V^b$ , where  $V^b$  is the trivial extension of  $V$ . We admit the possibility that  $D$  is a field,  $D$  is not integrally closed and  $F$  is not the quotient field of  $D$ . Therefore the class of rings considered in this context are more general than the classical Kronecker function rings and is in fact an instance of Halter-Koch's notion of an  $F$ -function ring.

A case of special interest is when we consider a field extension  $F/K$  that has at most countable transcendence degree and the ring  $D$  to be a finitely generated  $K$ -sub algebra of  $F$ . We define,

$$H := \bigcap_{V \in \Sigma(F/D)} V^b.$$

We investigate the ideal structure of  $H$  by using the topological structure of the Zariski-Riemann space  $\Sigma(F/D)$ . We show that for any pair of nonnegative integers  $d$  and  $h$  there are infinitely many prime ideals of dimension  $d$  and height  $h$  that are minimal over any proper nonzero finitely generated ideal of  $H$ . (Received August 21, 2008)