

1046-22-1130

**Lisa Carbone** and **Leigh Cobbs\*** (cobbs@math.rutgers.edu). *Infinite Towers of Cocompact Lattices in Kac-Moody Groups*. Preliminary report.

Let  $G$  be a locally compact Kac-Moody group of affine or hyperbolic type over a finite field  $\mathbb{F}_2$ . We suppose that  $G$  has type  $\infty$ , that is, the Weyl group  $W$  of  $G$  is a free product of  $\mathbb{Z}/2\mathbb{Z}$ 's. This includes all rank 2 and two possible rank 3 Kac-Moody groups. We show that if  $\text{rank}(G) = 2$  then  $G$  contains an infinite tower of non-conjugate cocompact lattices  $\dots \Gamma_3 \leq \Gamma_2 \leq \Gamma_1 \leq \Gamma$ , and we characterize the quotient graphs of groups  $\Gamma_i \backslash X$ . We also give sufficient conditions for extending coverings of edge-indexed graphs to covering morphisms of graphs of groups and we show how this gives rise to other infinite families of cocompact lattices in  $G$ . When  $\text{rank}(G) = 3$  we exhibit a subgroup  $\mathcal{Q}$  which contains a cocompact lattice  $\Lambda$  acting discretely and cocompactly on a simplicial tree  $\mathcal{X}$ . We exhibit an infinite tower of cocompact lattices  $\dots \Lambda_3 \leq \Lambda_2 \leq \Lambda_1 \leq \Lambda$  in  $\mathcal{Q}$  whose images in  $G$  are also discrete. This induces a tower of non-discrete subgroups  $\dots \Lambda'_3 \leq \Lambda'_2 \leq \Lambda'_1 \leq \Lambda$  in  $G$  for which we can characterize the quotient complexes of groups. (Received September 14, 2008)