James R. Gillespie* (jrg21@psu.edu). Gorenstein model structures and generalized derived categories.

We will see how the derived category of a ring can be constructed using Gorenstein homological algebra. Furthermore, this approach points to a theory of generalized derived categories. The method is to put a model structure on the category of graded $S[x]/(x^2)$ -modules where S is a Gorenstein ring. Taking S to be the integers, the model structure can then be lifted to $R[x]/(x^2)$ -modules where R is any ring. Its homotopy category recovers the derived category of R. By replacing $S[x]/(x^2)$ with other graded Gorensein rings, we are led to various generalizations of the usual derived category. We will give examples involving double complexes, and what we call k-chain complexes. (Received August 08, 2008)