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**William M. Wagner\*** ([wwagner1@columbus.rr.com](mailto:wwagner1@columbus.rr.com)), c/o Kathryn L. Wagner, 7199 Dublin Rd., Dublin, OH 43017-1164. *Continual Compounding of a Conventional Mortgage.*

Definitions:

L: Mortgage Loan; e.g. \$100,000.

T: Term in periodic units of time; e.g. 15 years.

R%: Rate of periodic interest; e.g. 6% per annum.

A: Amount of payment due at the end of one unit of time.

P: Instantaneous Principal.

The recursion relation for discrete compounding is  $P(i + 1) = P(i)[1 + R\%/m]$  where  $m$  is the number of payments (intervals) per unit of time; compounding occurs at the end of each such interval. As the cycle,  $(1/m)$ , of compounding and payments approaches infinity, the resulting limit is the first order linear Ordinary Differential Equation:  $-dP/dt = -R\%P + A$  The Integration Factor for this O.D.E. is  $EXP(-R\%t)$ . It shall be shown that:

I. The amplication factor of the Loan for total payments is  $(AT/L) = R\%T/[1 - EXP(-R\%T)]$ ; (Here, the total payment is \$151,660.60-.)

II.  $\text{Integral } [0, T; (-R\%P + A)] = L$ ; (This is analogous to the fact that, under discrete existense, the sum of the reductions in principal is equal to the Loan.)

III. The total interest  $(AT - L) = R\% \text{Integral}[0, T; P]$ . (Received August 10, 2008)