Meeting: 1005, Newark, Delaware, SS 16A, Special Session on Probabilistic Paradigms in Combinatorics

1005-05-163 Jacques A Verstraete* (jverstra@math.uwaterloo.ca), Faculty of Mathematics, University of Waterloo, 200 University Avenue West, Waterloo, Ontario N2L 3G1, Canada, Jeong Han Kim, Microsoft Research, One Microsoft Way, Redmond, WA 98052-6399, and Bela Bollobas,
Department of Mathematical Sciences, The University of Memphis, Memphis, TN 38152-3240.
Regular Subgraphs of Random Graphs.
We prove that there exists a function $\rho_{k}=(4+o(1)) k$ such that $G(n, \rho / n)$ contains a $k$-regular graph with high probability whenever $\rho>\rho_{k}$. In the case of $k=3$, it is also shown that $G(n, \rho / n)$ contains a 3 -regular graph with high probability whenever $\rho>\lambda \approx 5.1494$. These are the first constant bounds on the average degree in $G(n, p)$ for the existence of a $k$-regular subgraph. We also discuss the appearance of 3 -regular subgraphs in cores of random graphs. It is not known whether the $k+1$-core of a random graph when it exists contains a $k$-regular subgraph with high probability. (Received February 07, 2005)

