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The 3-colored Ramsey Number of Odd Cycles.
For graphs $L_{1}, \ldots, L_{k}$, the Ramsey number $R\left(L_{1}, \ldots, L_{k}\right)$ is the minimum integer $N$ satisfying that for any coloring of the edges of the complete graph $K_{N}$ on $N$ vertices by $k$ colors there exists a color $i$ for which the corresponding color class contains $L_{i}$ as a subgraph.

In 1973, Bondy and Erdős conjectured that if $n$ is odd and $C_{n}$ denotes the cycle on $n$ vertices, then $R\left(C_{n}, C_{n}, C_{n}\right)=$ $4 n-3$. In 1999, Luczak proved that $R\left(C_{n}, C_{n}, C_{n}\right)=4 n+o(n)$, where $o(n) / n \rightarrow 0$ as $n \rightarrow \infty$. In this paper we strengthen Łuczak's result and verify this conjecture for $n$ sufficiently large. (Received February 08, 2005)

