

**Meeting:** 1005, Newark, Delaware, SS 1A, Special Session on Homotopy Theory (in Honor of Donald M. Davis's and Martin Bendersky's 60th Birthdays)

1005-55-55            **Joseph Roitberg\*** ([roitberg@math.hunter.cuny.edu](mailto:roitberg@math.hunter.cuny.edu)), Department of Mathematics & Statistics, Hunter College, CUNY, 695 Park Avenue, New York, NY 10021, and **Yael Roitberg** ([yroitber@nyit.edu](mailto:yroitber@nyit.edu)), Department of Mathematics, New York Institute of Technology, Old Westbury, NY 11568. *Revisiting an example of Frank and Kahn.*

Let  $X$  be a pointed, finite CW-complex,  $\text{Aut}(X)$  the group of pointed homotopy classes of self-equivalences of  $X$  and  $\text{Aut}^*(X)$  the subgroup consisting of those elements of  $\text{Aut}(X)$  inducing the identity on all the integral homology groups of  $X$ . The classical finiteness theorems of Wilkerson, Sullivan and Dror-Zabrodsky, valid for 1-connected  $X$ , fail miserably in general. In an effort to formulate conjectures in the case where  $X$  is the wedge sum of a 1-connected, finite CW-complex and a finite collection of 1-spheres, we examine the case  $W =$  the wedge sum of a 1-sphere, a 2-sphere and a 3-sphere. In 1977, David Frank and Donald Kahn proved that neither  $\text{Aut}(W)$  nor  $\text{Aut}^*(W)$  is finitely generated. We prove:

Theorem: (i)  $\text{Aut}^*(W)$  is not nilpotent - nor even locally nilpotent; (ii)  $\text{Aut}^*(W)$  is metabelian; (iii)  $\text{Aut}^*(W)$  is both residually nilpotent and residually finite; (iv)  $\text{Aut}(W)$  is residually finite. (Received January 22, 2005)