Meeting: 1001, Evanston, Illinois, SS 8A, Special Session on Computability Theory and Applications

1001-03-82Wesley Calvert\*, Department of Mathematics, 255 Hurley Hall, University of Notre Dame,<br/>Notre Dame, IN 46556, and Valentina Harizanov, Julia F. Knight and Sara Miller.<br/>Description and Comparison of Computable Structures. Preliminary report.

I will address two related questions which arise in computable model theory. First, given a computable structure, what is its simplest description, up to isomorphism? Second, given some class of computable structures, how difficult is it to distinguish nonisomorphic members?

In particular, let K be a class of computable structures, and let I(K) denote the set of indices for members of K. We write  $I(\mathcal{A})$  for the set of indices for a structure  $\mathcal{A}$ . Write E(K) for the set of ordered pairs from I(K) which index isomorphic members of K. Now, if  $\mathcal{A}$  is computable,  $I(\mathcal{A})$  is  $\Sigma_1^1$ , and if I(K) is hyperarithmetical, then E(K) is  $\Sigma_1^1$ .

Often when E(K) is complete at some level (for instance,  $\Pi_3^0$ ), this completeness is witnessed by  $I(\mathcal{A})$  for some  $\mathcal{A} \in K$ . It is interesting to explore when there is such a witness. It is also interesting that for some K, any member will work as such a witness. Several examples will be given to illustrate these phenomena. (Received August 10, 2004)