Meeting: 1001, Evanston, Illinois, SS 5A, Special Session on Codes and Applications

1001-94-335 Mona Musa\* (mmusa@siue.edu), Department of Mathematics and Statistics, College of Arts and Sciences, Southern Illinois University Edwardsville, Edwardsville, IL 62026. On the double circulant presentation of the binary extended quadratic residue code. Preliminary report.

Let p be a prime such that  $p \equiv -1 \mod 8$ . Let k = (p+1)/2 and write  $k = 2^m q$ , q odd. Let  $S = F_2[x]/\langle 1 + x^k \rangle$  where  $F_2$  is the Galois field of two elements. We prove that the binary extended quadratic residue codes of length 2k have a double circulant presentation in the following three cases: (1) q = 1. (2) q is a prime and 2 is a primitive root modulo q. (3) Let X be the class of x in S, and  $\sigma$  the algebra of automorphisms on S that sends  $X^i$  to  $X^{-i}$ . Factor  $1 + x^q$  over  $F_2$  into irreducible factors. If the class of those factors in S is fixed by  $\sigma$  up to a unit, then the codes have a double circulant presentation. (Received August 30, 2004)