Meeting: 1004, Bowling Green, Kentucky, SS 6A, Special Session on Representation Theory

1004-17-81Jeb F. Willenbring\* (jw@uwm.edu), Department of Mathematical Sciences, P. O. Box 0413,<br/>Milwaukee, WI 53201-0413, and Gregg Zuckerman, Mathematics Dept., PO Box 208283, New<br/>Haven, CT 06520-8283. Small semisimple subalgebras of semisimple Lie algebras.

We study certain questions about the decomposition of a representation of a semisimple Lie algebra when restricted to a semisimple subalgebra. Specifically, we discuss a proof of the following theorem: let  $\mathfrak{k}$  be an  $\mathfrak{sl}_2$ -subalgebra of a semisimple Lie algebra  $\mathfrak{g}$ , none of whose simple factors is of type  $A_1$ . Then there exists a positive integer b, such that for every irreducible finite dimensional  $\mathfrak{g}$ -module V, there exists an injection of  $\mathfrak{k}$ -modules,  $W \to V$ , where W is an irreducible  $\mathfrak{k}$ -module of dimension less than b. The hypothesis of this result may be modified to obtain a result for an arbitrary semisimple Lie subalgebra  $\mathfrak{k}$ . In order to explain this modification, we introduce the notion of a *small subalgebra* of  $\mathfrak{g}$ . (Received January 17, 2005)