

Meeting: 1004, Bowling Green, Kentucky, SS 8A, Special Session on Topology, Convergence, and Order, in Honor of Darrell Kent

1004-54-42 **Anthony W. Hager*** (ahager@wesleyan.edu), Dept. of Math. and C.S., Wesleyan Univ., Middletown, CT 06459, and **Richard N. Ball.** *Epi-convergence and -topology in archimedean lattice-ordered groups.*

The category \mathcal{W} of archimedean l -groups with distinguished weak order unit includes all $C(X)$'s, all structures of real measurable functions mod null functions, etc. (with natural morphisms). Like any category, \mathcal{W} has its epimorphisms (right-cancelable), which we have studied previously; there is a rich theory. Now we construct and study two set-preserving functors out of \mathcal{W} : t , to semi-separated topological spaces; a , to Hausdorff convergence spaces. These are closely related to compact-open topology and convergence. For each B , the closure operators for $a(B)$ and for $t(B)$ coincide, and this closure captures epis in the sense: If a subobject A of B is dense, then A is epically embedded in B ; conversely when A is divisible. Sometimes, not always, $(B, t(B))$ is Hausdorff, or a topological l -group. Always, $(B, a(B))$ is a Hausdorff convergence l -group. The superiority of the theory in Convergence Spaces can be traced to the behavior of suprema in the lattice of convergences on a set: the sup of products is the product of sups. (Received January 10, 2005)