Meeting: 1004, Bowling Green, Kentucky, SS 4A, Special Session on Knot Theory and Its Applications

1004-57-234 Yuanan Diao^{*} (ydiao@uncc.edu), Department of Mathematics and Statistics, UNC Charlotte, Charlotte, NC 28223, and Claus Ernst and Uta Ziegler. The ropelength of closed braids. Preliminary report.

For a knot or link K, let L(K) denote the rope length of K and let Cr(K) denote the crossing number of K. An important problem in geometric knot theory concerns the bound on L(K) in terms of Cr(K). It is well known that there exist positive constants c_1 , c_2 such that for any knot or link K, $c_1 \cdot (Cr(K))^{3/4} \leq L(K) \leq c_2 \cdot (Cr(K))^{3/2}$. It is also known that for any real number p such that $3/4 \leq p \leq 1$, there exists a family of knots $\{K_n\}$ with the property that $Cr(K_n) \to \infty$ (as $n \to \infty$) such that $L(K_n) = O(Cr(K_n)^p)$. In this talk, we show that the power $(Cr(K))^{3/2}$ can be further reduced if the link K has a closed braid form such that the number of crossings in the braid is of the same order as Cr(K). (Received January 25, 2005)