Meeting: 1006, Lubbock, Texas, SS 5A, Special Session on Recent Advances in Complex Function Theory

 1006-30-93
Peter Duren* (duren@umich.edu), Department of Mathematics, University of Michigan, Ann Arbor, MI 48109-1109, Martin Chuaqui, Facultad de Matemáticas, P. Universidad Católica de Chile, Casilla 306, Santiago, Chile, and Brad Osgood, Department of Electrical Engineering, Stanford University, Stanford, CA 94305. A Schwarzian derivative criterion for univalence of harmonic mappings.

The Schwarzian derivative of a complex-valued harmonic function f can be defined in relation to its Weierstrass-Enneper lift F to a minimal surface Σ . We give a sufficient condition for the univalence of F in terms of the Schwarzian of f and the Gauss curvature K of Σ . Examples show that the condition is sharp. If f is analytic, then Σ is the complex plane, K = 0, and our condition reduces to a well known theorem of Nehari (1954). (Received February 08, 2005)