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**Glenn G Chappell** (chappellg@member.ams.org) and **Michael J Pelsmajer\***  
(pelsmajer@iit.edu), 10 W. 32nd St., E1 208, Chicago, IL 60616. *Maximum Induced Forests in  
Graphs of Bounded Treewidth.*

Let  $f_{k,d,n}$  be the maximum  $i$  such that every  $n$ -vertex graph of treewidth  $k$  contains an  $i$ -vertex induced forest of maximum degree at most  $d$ . We prove that for all  $k, d \geq 2$  and for all  $n \geq 1$ ,  $f_{k,d,n} \geq \lceil (2dn + 2)/(kd + d + 1) \rceil$  unless  $G \in \{K_{2,3}, K_{1,1,3}\}$  and  $k = d = 2$ . We give examples that show that the bound is sharp to within 1.

We conjecture that  $f_{k,1,n} \geq \lceil 2n/(k + 2) \rceil$ , which would be sharp to within 1, and we prove it for  $k = 2, 3$ . For  $k \geq 4$ , we show that  $f_{k,1,n} \geq (2n + 2)/(2k + 3)$ . We also determine  $f_{k,d,n}$  when  $d = 0$  or  $k = 0, 1$ . Finally, we consider an analogue of  $f_{k,d,n}$  for graphs on a given surface, rather than graphs of a given treewidth. (Received September 22, 2009)