1056-05-519 Bruce E Sagan\* (sagan@math.msu.edu), Department of Mathematics, Michigan State University, East Lansing, MI 48824. Probabilistic proofs of hook length formulas involving trees. Let T be a rooted tree with n vertices. We use T to stand for the vertex set of T. An increasing labeling of T is a bijection  $\ell: T \to \{1, 2, ..., n\}$  such that  $\ell(v) \leq \ell(w)$  for all descendents w of v. Let  $f^T$  be the number of increasing labelings. The hooklength,  $h_v$ , of a vertex v is the number of descendents of v. The hook length formula for trees is

$$f^T = \frac{n!}{\prod_{v \in T} h_v}.$$

There is a similar formula for the number of standard Young tableaux of given shape. Greene, Nijenhuis, and Wilf gave a beautiful probabilistic proof of the tableau formula where the hooklenths enter in a very natural way.

Recently, Han discovered a formula which has the interesting property that hooklengths appear as exponents. Specifically, let  $\mathcal{B}(n)$  be the set of all *n*-vertex binary trees. Han proved that

$$\sum_{T \in \mathcal{B}(n)} \prod_{v \in T} \frac{1}{h_v 2^{h_v - 1}} = \frac{1}{n!}$$

using algebraic manipulations. We will show how to give a simple probabilistic proof of this equation as well as various generalizations. We will also pose some open questions raised by this work. (Received September 11, 2009)