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Helen G Grundman^{*} (grundman[@]brynmawr.edu), Department of Mathematics, Bryn Mawr College, 101 N. Merion Ave., Bryn Mawr, PA 19010. Solutions to xyz = x + y + z = 1 in algebraic integers of bounded degrees. Preliminary report.

Several papers have considered the problem of finding, for a fixed $n \in \mathbb{Z}^+$, all integral solutions to xyz = x + y + z = 1 contained in fields of degree *n* over **Q**. Complete results are known for $n \leq 4$, but only partial results are known for n = 5. In particular, it is not known (or even conjectured) that, for n = 5, all of the solutions have been found.

In this talk, I will summarize the earlier findings for $n \leq 5$ and then discuss more recent work that has led to the discovery of further solutions to the equation in the quintic field case. I will also discuss the remaining roadblocks to completely solving the problem in this case. (Received September 17, 2009)