1056-12-688Ha N Nguyen* (hnnguye@emory.edu), 1506 Tuxworth Cir, Decatur, GA 30033, and Victoria
Powers (vicki@mathcs.emory.edu), 400 Dowman Dr., W401, Atlanta, GA 30322.
Representations of polynomials non-negative on non-compact subsets of \mathbb{R}^2 .

Recently, M. Marshall settled a long-standing question in real algebraic geometry by showing that if $f(x, y) \in \mathbb{R}[x, y]$ and $f(x, y) \geq 0$ on the strip $[0, 1] \times \mathbb{R}$, then f has a representation $f = \sigma_0 + \sigma_1 x(1 - x)$, where $\sigma_0, \sigma_1 \in \mathbb{R}[x, y]$ are sums of squares.

In this talk, we give the background to this result, which goes back to Hilbert's 17th problem, and our generalizations to other non-compact subsets of \mathbb{R}^2 . (Received September 15, 2009)