1056-20-277Joseph Kirtland* (joe.kirtland@marist.edu), Department of Mathematics, Marist College,
3399 North Road, Poughkeepsie, NY 12601. Finite Groups with Permutable Supplemented
Subgroups. Preliminary report.

A finite group G = ABC for subgroups A, B, and C of G if for each element $g \in G$, then g = abc where $a \in A, b \in B$, and $c \in C$. A finite group G = (AB)C if G = ABC and AB is a subgroup of G. However, if G = (AB)C it does not imply that G = A(BC) or that BC is a subgroup of G. This talk will investigate groups which do satisfy this transitivity condition (G = (AB)C implies G = A(BC)) for proper subgroups. This examination will lead to a study of p-groups in which each subgroup not contained in the Frattini subgroup permutes with every other subgroup in the group. (Received August 24, 2009)