Matthew Rudd* (mrudd@uidaho.edu), Department of Mathematics, University of Idaho, 300 Brink Hall, Moscow, ID 83844. Statistics of p-harmonic functions. Preliminary report.

The mean value property characterizes continuous harmonic functions, and it is natural to wonder if p-harmonic functions have analogous statistical descriptions. Some basic calculations suggest that a continuous function u is p-harmonic in Ω if and only if

$$u(x) = (2 - p) \text{ median } \{ u(s) \} + (p - 1) \text{ mean } \{ u(s) \}$$

at each $x \in \Omega$, where $s \in \partial B(x,r)$ and $B(x,r) \subseteq \Omega$. We will report on ongoing work on these ideas and their applications. (Received September 22, 2009)