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Abdulkadir Dogan and John R Graef<sup>\*</sup> (John-Graef@utc.edu), Department of Mathematics, The University of Tennessee at Chattanooga, Chattanooga, TN 37403, and Lingju Kong. *Higher* order singular multi-point boundary value problems on time scales.

We study the singular boundary value problem

$$\left(\phi\left(u^{\Delta^{n-1}}\right)\right)^{\nabla} + \lambda a(t)f(u) = 0, \ t \in (0,T)_{\mathbb{T}},$$
$$\begin{cases} u^{\Delta^{i}}(0) = \sum_{j=1}^{m} \alpha_{j} u^{\Delta^{i}}(\xi_{j}), \ i = 0, \dots, n-2, \\ \phi\left(u^{\Delta^{n-1}}(T)\right) = \sum_{j=1}^{m} \beta_{j} \phi\left(u^{\Delta^{n-1}}(\xi_{j})\right), \end{cases}$$

on a time scale  $\mathbb{T}$ . Conditions for the existence and uniqueness of positive solutions are obtained. The dependence of positive solutions on the parameter  $\lambda$  is studied. We also present similar results for a problem with the same differential equation and different boundary conditions. The results are illustrated with examples. Our analysis mainly relies on the mixed monotone operator theory. (Received September 16, 2009)