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When certain statements are provable in subsystems of constructive analysis using intuitionistic predicate calculus, related sequential statements are provable in weak classical subsystems. For example, for formulas Φ of a special sort, if a sentence $\forall X \exists Y \Phi(X, Y)$ is provable using $\mathbf{E-HA}^\omega$, then the related sequential form

$$\forall \langle X_n \mid n \in \mathbb{N} \rangle \exists \langle Y_n \mid n \in \mathbb{N} \rangle \forall n \phi(X_n, Y_n)$$

is provable in \mathbf{RCA} . We call our theorems “uniformization results” because the provability of the sequential form demonstrates a kind of uniformity in the proof of the original sentence. The contrapositives of these uniformization results allow us to apply techniques of reverse mathematics to show the non-provability of statements in constructive axiom systems. (Received September 21, 2010)