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**Michel X. Goemans\*** ([goemans@math.mit.edu](mailto:goemans@math.mit.edu)), MIT, Room 2-351, 77 Massachusetts Ave., Cambridge, MA 02420. *Thin spanning trees, conductances, nowhere zero flows, and the traveling salesman problem.*

A spanning tree  $T$  in a graph  $G$  is  $\epsilon$ -thin if  $T$  contains at most an  $\epsilon$  fraction of the edges of every cut. Goddyn's conjecture says that every  $f(\epsilon)$ -edge-connected graph contains an  $\epsilon$ -thin tree for a suitable function  $f$ . In this talk, we discuss this conjecture and variants of it, and its implications for nowhere zero 3-flows and for the approximability of the asymmetric traveling salesman problem. In particular, we show that, if the graph is  $(c \log(n)/\log \log(n))$ -edge-connected, one can select conductances in a corresponding electrical network so that a random spanning tree is  $\epsilon$ -thin with high probability. We also show that, if we replace the spanning tree requirement by simply having a linear number of edges then Goddyn's conjecture can be proved. (Received September 17, 2010)