Darren A. Narayan* (dansma@rit.edu), School of Mathematical Sciences, 85 Lomb Memorial Drive, Rochester Institute of Technology, Rochester, NY 14623, and Robert Jamison.
Max-optimal and sum-optimal labelings of graphs.
A $k$-ranking of a graph is a labeling of its vertices with $k$ positive integers such that any path between two vertices with the same label contains a vertex with a larger label. A $k$-ranking is minimal if the reduction of any label greater than 1 violates the described ranking property. We consider two norms for minimal rankings. The max-optimal norm is the smallest $k$ for which $G$ has a minimal $k$-ranking. This value is also referred to as the rank number. In this talk we consider the sum-optimal norm in which the sum of all labels over all minimal rankings is minimized. We investigate similarities and differences between the two norms. In particular we show that sum-optimal rankings of paths and cycles are also max-optimal. (Received September 20, 2010)

