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Let  $f(n, p, q)$  be the minimum number of colors necessary to color the edges of  $K_n$  so that every  $K_p$  is at least  $q$ -colored. We improve current bounds on these nearly “anti-Ramsey” numbers, first studied by Erdős and Gyárfás. We show that  $f(n, 5, 9) \geq \frac{7}{4}n - 3$ , slightly improving the bound of Axenovich. We make small improvements on bounds of Erdős and Gyárfás by showing  $\frac{5}{6}n + 1 \leq f(n, 4, 5)$  and for all even  $n \not\equiv 1 \pmod{3}$ ,  $f(n, 4, 5) \leq n - 1$ . For a complete bipartite graph  $G = K_{n,n}$ , we show an  $n$ -color construction to color the edges of  $G$  so that every  $C_4 \subseteq G$  is colored by at least three colors. This improves the best known upper bound of M. Axenovich, Z. Füredi, and D. Mubayi. Keywords: Ramsey theory, generalized Ramsey theory, rainbow-coloring, edge-coloring, Erdős problem

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