

1067-05-359

**Eva K. Belmont\*** (ebelmont@fas.harvard.edu), Department of Mathematics, FAS, Harvard University, 1 Oxford St., Cambridge, MA 02138. *Paths as  $m$ -step Competition Graphs.*

For any digraph  $D$  let the  $m$ -step competition graph  $C^m(D)$  be the graph with the same vertices as  $D$ , where  $x$  and  $y$  are connected in  $C^m(D)$  if there are  $m$ -step paths in  $D$  from  $x$  and  $y$  to a common vertex  $z$ . G.T. Helleloid (2005) showed that if  $m \geq n$ , then the path  $P_n$  on  $n$  vertices is not an  $m$ -step competition graph for any digraph  $D$ . J. Kuhl and B.C. Swan (2010) showed that  $P_n$  is not an  $m$ -step competition graph for  $\frac{n}{2} \leq m \leq n - 3$ , and that  $P_n$  is an  $m$ -step competition graph if either  $m|n - 1$  or  $m|n - 2$ . We show that these conditions are necessary; that is,  $P_n$  is an  $m$ -step competition graph if and only if the aforementioned divisibility conditions hold. (Received August 26, 2010)