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A coloring of the vertices of a hypergraph \mathcal{H} is called *conflict free* if each edge e of \mathcal{H} contains a vertex whose color does not get repeated in e. The smallest number of colors required for such a coloring is called the conflict-free chromatic number of \mathcal{H} , and is denoted by $\chi_{CF}(\mathcal{H})$. Pach and Tardos studied this parameter for graphs and hypergraphs. Among other things, they proved that for an (2r-1)-uniform hypergraph \mathcal{H} with m edges, $\chi_{CF}(\mathcal{H})$ is of the order of $m^{1/r} \log m$. They also raised the question whether the same result holds for r-uniform hypergraphs. In this talk we shall show that this is not necessarily true. Moreover, we provide lower and upper bounds on the minimum number of edges of an r-uniform simple hypergraph which is not conflict free k-colorable. This is a joint work with A. Kostochka and T. Łuczak. (Received September 10, 2010)