1067-11-1462Paul Jenkins and Jeremy Rouse* (rouseja@wfu.edu), Department of Mathematics, Wake
Forest University, P.O. Box 7388, Winston-Salem, NC 27109. Modular forms with non-negative
Fourier coefficients and extremal lattices.

If

$$f(z) = \sum_{n=1}^{\infty} a(n)q^n$$

is a cusp form of weight k for the full modular group it is known that there is a constant C_f so that

$$|a(n)| \le C_f d(n) n^{\frac{k-1}{2}}$$

Such a form f(z) is determined by its first $\ell = \lceil \frac{k}{12} \rceil$ coefficients, and our first main result is a bound on C_f in terms of $a(1), a(2), \ldots, a(\ell)$.

We apply this result to the study of extremal lattices. The theta function of such a lattice will be the unique (non-cuspidal) modular form of weight k with

$$f(z) = 1 + O(q^{\ell+1})$$

and will have non-negative coefficients. We show that the form f(z) has non-negative coefficients when k = 81632, but that some coefficients are negative when k = 81644. (Received September 21, 2010)