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Paul Pollack* (pppollac@illinois.edu), 1409 W. Green St., Department of Mathematics, MC-382, University of Illinois, Urbana, IL 61801. *Sociable numbers, or* How I messed with perfection and lived to write papers about it.

Let $s(n) := \sum_{d|n,d < n} d$ denote the sum of the proper divisors of the natural number n. We call n perfect if s(n) = n. The study of such numbers goes back thousands of years, but many of the most natural questions remain unanswered. Similar comments apply to the study of *amicable pairs*, which are pairs of natural numbers n and m for which s(n) = m while s(m) = n. (In this case, both n and m are called *amicable numbers*.) I will describe recent results concerning perfect numbers, amicable numbers, and their higher-order generalizations, so-called *sociable numbers*. (Received September 22, 2010)