## 1067-13-1777 Witold Kraskiewicz, Instytut Matematyki UMK, ul. Chopina 12/18, 87100 Torun, Poland, and Jerzy Weyman\*, 360 Huntington Av., Boston, MA 02115. *Finite free resolutions of varieties with symmetries.* Preliminary report.

Let g be a simple Lie algebra, and  $\alpha$  in g a simple root. The root  $\alpha$  defines a grading on g. We are interested in the action of group  $G_0$  of the Lie algebra  $g_0$  on the space  $g_1$ . Such representations are closely related to irreducible representations of simple Lie algebras with finitely many orbits. It is well known that the action of  $G_0 \times C^*$  on  $g_1$  has finitely many orbits. By using geometric invariant theory we calculate Hilbert polynomials of (normalizations) of orbit closures. In many cases we can deduce normality, Cohen-Macaulay and Gorenstein properties of the orbit closures. This technique gives several cases of interesting pure resolutions. I will also describe the link of such constructions to the structure theorems on finite free resolutions of length three. (Received September 21, 2010)