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**Lance Bryant\*** (lbryant@ship.edu), Mathematics Department, Shippensburg University, 1871 Old Main Dr, Shippensburg, PA 17257, and **James Hamblin** and **Lenny Jones**. *Unique Maximal-Length Factorization in Numerical Semigroups*. Preliminary report.

A numerical semigroup  $S = \langle n_1, n_2, \dots, n_t \rangle$  is a subset of the natural numbers including 0 such that  $0 \in S$ ,  $S$  is closed under addition, and  $S$  has finite complement in the natural numbers. We say  $n_1, n_2, \dots, n_t$  are the minimal generators of  $S$ , i.e.,  $S = \{\sum c_i n_i \mid c_i \geq 0\}$  and any other set of generators contains this set. An element  $s \in S$  may be able to be expressed as a nonnegative linear combination of the minimal generators (called a factorization) in several ways. A maximal-length factorization is one that requires the most minimal generators. For example, in  $S = \langle 7, 10, 13 \rangle$ , we have  $62 = 10 + 13 + 13 + 13 + 13 = 7 + 7 + 7 + 7 + 7 + 7 + 10 + 10 = 7 + 7 + 7 + 7 + 7 + 7 + 7 + 13$ . Thus 62 has three factorization and the last two are maximal-length factorizations. This talk will focus on maximal-length factorizations when  $S$  has three minimal generators with particular interest in when every element of  $S$  has exactly one maximal-length factorization. (Received September 22, 2010)