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Vector spaces over the binary field \mathbb{Z}_2 share certain properties with familiar vector spaces over \mathbb{R} such as the existence of bases for spaces. There are, however, many differences. For example, when equipped with the dot product, a vector space over \mathbb{Z}_2 becomes an indefinite inner product space where non-zero vectors may have zero length. We continue previous work on these spaces by investigating subspaces of \mathbb{Z}_2^n and ask when two vector spaces are unitarily equivalent. In particular we consider embeddings of subspaces into \mathbb{Z}_2^n for some n . An algorithm is given showing that every vector space over \mathbb{Z}_2 can be embedded in this manner. We also investigate the existence of both Parseval frames and dual frames for vector spaces over \mathbb{Z}_2 and their relation to the Gramian operator. Finally we show that, unlike vector spaces over \mathbb{R} , the existence of a dual frame pair does not necessarily imply the existence of a Parseval frame of the same length for a space. (Received July 26, 2010)