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Earl J. Taft* (etaft@math.rutgers.edu), Department of Mathematics, Rutgers University, Piscataway, NJ 08854, and **Zhifeng Hao** (mazfhao@scut.edu.cn), Department of Mathematical Science, South China University of Technology, Guangzhou, 510640. *The Lie product in the continuous Lie dual of the Witt algebra.*

Let k be a field of characteristic zero. The simple Lie algebra $W_1 = \text{Der } k[x]$, the one-sided Witt algebra, has a basis $e_i = x^{(i+1)}d/dx$ for i at least -1 . For each i , the wedge of e_0 and e_i satisfies the classical Yang-Baxter equation, giving W_1 the structure of a coboundary triangular Lie bialgebra $(W_1)^{(i)}$. The continuous Lie dual of $(W_1)^{(i)}$ is also a Lie bialgebra, and has been identified with the space of k -linearly recursive sequences by W. Nichols [J. Pure Appl. Alg. 68(1990), 359-364]. Let $f = (f_n)$ and $g = (g_n)$ be linearly recursive sequences in the continuous linear dual of $(W_1)^{(i)}$, $[f, g]$ their Lie product. For each n , the n -th coordinate of $[f, g]$ has been described in terms of the coordinates of f and of g [E. J. Taft, J. Pure Appl. Alg. 87(1993), 301-312], but it was an open problem to give a recursive relation satisfied by $[f, g]$ in terms of recursive relations satisfied by f and by g . We give such a relation here. Analogous results hold for the two-sided Witt algebra $W = \text{Der } k[x, x^{(-1)}]$. (Received August 05, 2010)