1067-20-2285 **Thomas Koberda*** (koberda@math.harvard.edu), Department of Mathematics, Harvard University, 1 Oxford St., Cambridge, MA 02138. *Faithful actions of automorphisms on the space of* orderings of a group.

We study the space of left– and bi–invariant orderings on a torsion–free nilpotent group G. We will show that generally the set of such orderings is equipped with a faithful action of the automorphism group of G. We prove an extension result which allows us to establish the same result when G is assumed to be merely residually torsion–free nilpotent. In particular, we obtain faithful action of mapping class groups of surfaces. We will draw connections between the structure of orderings on residually torsion–free nilpotent, hyperbolic groups and their Gromov boundaries, and we show that in those cases a faithful Aut(G)–action on the boundary is equivalent to a faithful Aut(G) action on the space of left–invariant orderings. (Received September 22, 2010)