Quasi-analytic classes of functions with super-exact asymptotic expansions arise in Ilyashenko's solution of Dulac's problem. We hope to prove that some of these classes generate o-minimal structures. These structures would be exponentially, but not polynomially, bounded. I will describe Ilyashenko's construction and outline our plan for proving o-minimality. (Received September 15, 2010)

