

1067-32-1554

Jerry R. Muir, Jr.* (muirj2@scranton.edu), Department of Mathematics, University of Scranton, Scranton, PA 18510. *The Roles Played by Order of Convexity or Starlikeness and the Bloch Condition in the Extension of Mappings from the Disk to the Ball*. Preliminary report.

Given f , a normalized ($f(0) = 0$, $f'(0) = 1$) locally univalent function defined on the open unit disk of \mathbb{C} , we consider the extension of f to the open unit ball of \mathbb{C}^n given by $F(z) = (f(z_1) + G(\sqrt{f'(z_1)} \hat{z}), \sqrt{f'(z_1)} \hat{z})$, $\hat{z} = (z_2, \dots, z_n) \in \mathbb{C}^{n-1}$. Here G is a complex-valued holomorphic function defined on a ball in \mathbb{C}^{n-1} of possibly infinite radius centered at 0 such that $G(0) = 0$ and $DG(0) = 0$. It is known that, if f is convex or starlike (univalent), then F inherits the same property when G is a homogeneous polynomial of degree 2 of sufficiently small norm. We consider what additional conditions on f will allow for G to have terms of degree greater than 2 in its expansion about 0 and have F still possess the relevant geometric property. (Received September 21, 2010)