

1067-34-379

**A Peterson\*** (apeterso@math.unl.edu), Department of Mathematics, University of Nebraska-Lincoln, Lincoln, NE 68588. *Asymptotic behavior of an n-th order sublinear dynamic equation.*

In this paper, we study the asymptotic behavior of the following n-th order sublinear dynamic equation

$$x^{\Delta^n}(t) + p(t)x^\alpha(t) = 0, \quad 0 < \alpha < 1,$$

where  $p \geq 0$ , on an isolated time scale  $\mathbb{T}$ , and  $\alpha$  is a ratio of odd positive integers. As an application, we obtain

(i) when  $n$  is even, every solution  $x(k)$  of the difference equation

$$\Delta^n x(k) + p(k)x^\alpha(k) = 0, \quad 0 < \alpha < 1,$$

where  $p(k) \geq 0$ , is oscillatory if and only if

$$\sum_{k=1}^{\infty} k^{\alpha(n-1)} p(k) = \infty.$$

(ii) when  $n$  is odd, every solution  $x(k)$  of the difference equation is either oscillatory or  $\lim_{k \rightarrow \infty} x(k) = 0$  if and only if the above sum diverges. (Received August 30, 2010)