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**Claude Bardos** ([claude.bardos@gmail.com](mailto:claude.bardos@gmail.com)), Laboratory J.L.Lions, University of Pierre and Marie Curie, 75013 Paris, France, and **Edriss S Titi\*** ([etiti@math.uci.edu](mailto:etiti@math.uci.edu)), Dept. of Computer Science and Applied Math, The Weizmann Institute of Science, 76100 Rehovot, Israel. *On the Loss of Regularity for the Three-Dimensional Euler Equations.*

A basic example of shear flow was introduced by DiPerna and Majda to study the weak limit of oscillatory solutions of the Euler equations of incompressible ideal fluids. In particular, they proved by means of this example that weak limit of solutions of Euler equations may, in some cases, fail to be a solution of Euler equations. We use this shear flow example to provide non-generic, yet nontrivial, examples concerning the loss of smoothness of solutions of the three-dimensional Euler equations, for initial data that do not belong to  $C^{1,\alpha}$ . Moreover, we show by means of this shear flow example the existence of weak solutions for the three-dimensional Euler equations with vorticity that is having a nontrivial density concentrated on non-smooth surface. This is very different from what has been proven for the two-dimensional Kelvin-Helmholtz problem where a minimal regularity implies the real analyticity of the interface. Eventually, we use this shear flow to provide explicit examples of non-regular solutions of the three-dimensional Euler equations that conserve the energy, an issue which is related to the Onsager conjecture. (Received September 18, 2010)