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Eunhyung Lee (eunhyung165@gmail.com) and **R. Shivaji** (shivaji@ra.msstate.edu). *A
multiplicity result for a class of infinite positone problems.*

We study positive solutions to the singular boundary value problem

$$\begin{cases} -\Delta_p u = \lambda \frac{f(u)}{u^\beta} & \text{in } \Omega, \\ u = 0 & \text{on } \partial\Omega, \end{cases}$$

where $\Delta_p u = \operatorname{div}(|\nabla u|^{p-2} \nabla u)$, $p > 1$, $\lambda > 0$, $\beta \in (0, 1)$ and Ω is a bounded domain in \mathbb{R}^N , $N \geq 1$. Here $f : [0, \infty) \rightarrow (0, \infty)$ is a continuous nondecreasing function such that $\lim_{u \rightarrow \infty} \frac{f(u)}{u^{\beta+p-1}} = 0$. We establish the existence of multiple positive solutions for certain range of λ when f satisfies certain additional assumptions. A simple model that will satisfy our hypotheses is $f(u) = e^{\frac{\alpha u}{\alpha+u}}$ for $\alpha \gg 1$. We also extend our results to classes of systems when the nonlinearities satisfy a combined sublinear condition at infinity. We prove our results by the method of sub-super solutions. (Received July 28, 2010)