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**Christopher J Winfield\*** (winfield@madscitech.org). *Local Solvability on  $\mathbb{H}_1$  :  
Non-homogeneous operators.* Preliminary report.

Local solvability and non-solvability are classified for certain operators which are left-invariant on the Heisenberg group  $\mathbb{H}_1$  of order  $n \geq 2$ . For a large subclass of our operators, (non-) solvability is determined by the highest order terms in  $X$  and  $Y$ . We study operators which can be written in form of polynomials with constant coefficients

$$P(X, Y) = P_n(X, Y) + Q(X, Y).$$

Here  $P_n$  is a homogeneous polynomial of degree  $n \geq 2$  in a certain broad (so-called "generic") class;  $Q$  is any such polynomial but of order less than  $n$ ; and,  $X, Y$  are the vector fields  $X = \partial_x, Y = \partial_y + x\partial_z$ .

Our operators can be viewed as perturbations of operators whose ( $\mathcal{C}^\infty$ ) solvability is already classified in the present representation:  $P_n(X, Y)$  is locally solvable if and only if the adjoint operators of both  $\ker P(\pm i\partial_t, t)$  contain only the zero function. The solvability in our more general class is examined via asymptotic estimates of solutions certain ode's with a large parameter, analytic extensions of such solutions and a classification of related scattering matrices. (Received September 10, 2010)