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We consider certain matrix difference equations, where the eigenvalues of the 2×2 transition matrix are distinct. As usual, diagonalization gives the solution involving (the real and imaginary parts of) powers of an eigenvalue λ . Whether the argument $\alpha > 0$ of λ is an irrational multiple of π and whether $|\lambda| > 1$, $= 1$, or < 1 , govern the type of long-term behavior. Various cases are illustrated when the starting values compare differently with the equilibrium values. Plane quadrants where each component of the solution is increasing/decreasing and is greater/less than its counterpart in the equilibrium are identified. Actually when both starting values are different from such counterparts, the quadrants are obtained from the ordinary ones via a certain rotation. These are implied by the Beatty sequence $[n\alpha]$, and in the latter case by the more general Sturmian sequence $[\gamma + n\alpha]$, $n \in \mathbb{N}$, where γ is described. Anyone who ever built numerical solutions to such systems and wondered why, for some k , they oscillated every k or $k - 1$ terms, now sees how k relates to α . (Received July 31, 2010)