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**Judith A. Packer\*** ([packer@colorado.edu](mailto:packer@colorado.edu)), Department of Mathematics, CB 395, University of Colorado at Boulder, Boulder, CO 80309-0395. *Tensor products of generalized multiresolution analyses*. Preliminary report.

Consider a generalized multiresolution analysis (GMRA)  $(\{V_j\}, \pi, \delta)$  for a discrete abelian group and non-surjective automorphism pair  $(\Gamma, \alpha)$ , where  $\alpha(\Gamma)$  has finite index in  $\Gamma$  and  $\bigcap_{n=0}^{\infty}(\alpha^n(\Gamma)) = \{0_\Gamma\}$ . Here the  $V_j$  are nested subspaces of the Hilbert space  $\mathcal{H}$  satisfying the standard intersection and density conditions,  $\pi$  is a representation of  $\Gamma$  on  $\mathcal{H}$  with invariant subspace  $V_0$ ,  $\delta$  is a unitary dilation on  $\mathcal{H}$ , with  $\delta^1 \circ \pi_\gamma \circ \delta = \pi_{\alpha(\gamma)}$ . We discuss a recent construction of L. Baggett, V. Furst, K. Merrill, and the author, where we are given a system  $(\{V'_j\}, \pi', \delta)$  for a different discrete abelian group/automorphism pair  $(\Gamma', \alpha')$ , where we do not necessarily insist  $\bigcap_{j \in \mathbb{Z}} V'_j = \{0\}$ . We analyze some interesting examples and natural questions that arise when one constructs the Cartesian product  $(\Gamma \times \Gamma', \alpha \times \alpha')$  and the corresponding triple  $(\{V_j \otimes V'_j\}, \pi \otimes \pi', \delta \otimes \delta')$  in  $\mathcal{H} \otimes \mathcal{H}'$ . (Received September 19, 2010)