

1067-43-2240

**Nicholas Boros\*** (borosnic@msu.edu), 354 Lamb Street, Perry, MI 48872. *Sharp  $L^p$ -bounds for a perturbation of Burkholder's Martingale Transform.*

In this talk we discuss how to find the Bellman function associated with proving the following estimate. For  $1 < p < \infty$ ,  $\tau \in [-\frac{1}{2}, \frac{1}{2}]$ ,  $\varepsilon_k \in \{\pm 1\}$ ,  $n \in \mathbb{Z}_+$ ,  $\{d_k\}_k$  a martingale difference sequence and  $\begin{pmatrix} \varepsilon_k \\ \tau \end{pmatrix}$  a vector in  $\mathbb{R}^2$ , we obtain

$$\left\| \sum_{k=1}^n \begin{pmatrix} \varepsilon_k \\ \tau \end{pmatrix} d_k \right\|_{L^p([0,1], \mathbb{C}^2)} \leq C_{p,\tau} \left\| \sum_{k=1}^n d_k \right\|_{L^p([0,1], \mathbb{C})},$$

with  $C_{p,\tau}$  as the sharp constant. This is a generalization of Burkholder's famous result, which holds when  $\tau = 0$  with  $C_{p,\tau} = \max\{p - 1, \frac{1}{p-1}\}$ , that can similarly be used to obtain sharp estimates of singular integrals. We discuss an application to a singular integral which has an operator norm of  $C_{p,\tau}$ . This is a joint work with P. Janakiraman and A. Volberg. (Received September 22, 2010)