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The Segal-Bargmann projection is a projection $P_\alpha : L^2(\mu_\alpha) \rightarrow \mathcal{HL}^2(\mu_\alpha)$, where α is any positive real number, μ_α is a Gaussian measure on \mathbb{C}^n given by $d\mu_\alpha = \left(\frac{\alpha}{\pi}\right)^n e^{-\alpha|z|^2} dm$ (where dm is Lebesgue measure on \mathbb{C}^n), and $\mathcal{HL}^2(\mu_\alpha)$ is the space of functions in $L^2(\mu_\alpha)$ that are also holomorphic on \mathbb{C}^n . For $1 < p < \infty$, this projection can be extended to a bounded transformation $P_\alpha : L^p(\mu_{\alpha p/2}) \rightarrow \mathcal{HL}^p(\mu_{\alpha p/2})$. In fact, if we denote the norm of the above operator as $\|P_\alpha\|_{p \rightarrow p}$, it is not difficult to show that $\|P_\alpha\|_{p \rightarrow p} \leq 2^n$.

In this talk we will show that in the case $n = 1$, the norm $\|P_\alpha\|_{p \rightarrow p}$ can be computed exactly as $\|P_\alpha\|_{p \rightarrow p} = \frac{2}{p^{1/p} p'^{1/p'}}$, where p' is defined as $\frac{1}{p'} = 1 - \frac{1}{p}$. For $n > 1$, we will show that $\|P_\alpha\|_{p \rightarrow p} \geq \left(\frac{2}{p^{1/p} p'^{1/p'}}\right)^n$. (Received August 24, 2010)