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*Non-commutative Inequalities.*

The talk concerns inequalities for non-commutative functions. At this point we have for free  $*$ -algebras:

A. versions of the classical real algebraic geometry description of when one polynomial  $p$  is positive on the domain where another polynomial  $q$  is positive (due to a growing list of authors).

B. classification of convex non-commutative polynomials, rational functions and varieties. There are shockingly few. (due to Dym Hay Helton McCullough Vinnikov; algorithms for symbolic computation Camino, Helton, de Oliveira Shopp, Slingend).

C. some theory of changes of variables to achieve non-commutative convexity (due to Helton Klep McCullough Popescu).

D. other.

The talk will select a topic from this. The work originates in trying to develop some theory for studying the matrix inequalities which are ubiquitous in linear engineering systems and control. (Received September 12, 2010)