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**Tao Wang\*** ([wang\\_t@math.psu.edu](mailto:wang_t@math.psu.edu)), 402 McAllister BLDG, Department of Mathematics, university park, PA 16802, and **Alberto Bressan**. *The Minimum Speed for a Blocking Problem on the Half Plane*.

We consider a blocking problem: fire propagates on a half plane with unit speed in all directions. To block it, a barrier can be constructed in real time, at speed  $\sigma$ . We prove that the fire can be entirely blocked by the wall, in finite time, if and only if  $\sigma > 1$ .

The proof relies on a geometric lemma of independent interest. Namely, let  $K \subset R^2$  be a compact, simply connected set with smooth boundary. We define  $d_K(x, y)$  as the minimum length among all paths connecting  $x$  with  $y$  and remaining inside  $K$ . Then  $d_K$  attains its maximum at a pair of points  $(\bar{x}, \bar{y})$  both on the boundary of  $K$ . (Received September 22, 2010)