

1067-52-985

**Stoyu Barov** (stoyu@yahoo.com), Institute of Mathematics, Bulgarian Academy of Sciences, 8 Acad. G. Bonchev Str., 1113 Sofia, Bulgaria, and **Jan J. Dijkstra\*** (dijkstra@cs.vu.nl), Afdeling Wiskunde, Vrije Universiteit, De Boelelaan 1081, 1081 HV Amsterdam, Netherlands. *On closed sets with convex shadows in Hilbert space.*

For a subset of the Hilbert space  $\ell^2$  its *shadows* are the orthogonal projections of the set onto hyperplanes. If  $\mathcal{P}$  is a set of projection directions (unit vectors) then two sets are called  $\mathcal{P}$ -imitations of each other if they have identical shadows in all directions from  $\mathcal{P}$ . We present a number of results about closed sets in  $\ell^2$  that have convex shadows.

**Theorem 1.** *Let  $B$  be a closed convex subset of  $\ell^2$  that does not contain a hyperplane and let  $\mathcal{P}$  be a set of directions such that  $B$  is not an  $(\text{int } \overline{\mathcal{P}})$ -imitation of  $B$ . If  $C$  is a closed  $\mathcal{P}$ -imitation of  $B$  such that  $C \neq B$  then  $C$  contains a closed set that is homeomorphic to  $\ell^2$ .*

For a set  $B \subset \ell^2$  we let the *geometric interior* denote the interior of  $B$  with respect to the closed affine hull of  $B$ .

**Theorem 2.** *Let  $B$  be a closed convex subset of  $\ell^2$  with an empty geometric interior and let  $\mathcal{P}$  be a somewhere dense set of directions. If  $C$  is a closed  $\mathcal{P}$ -imitation of  $B$  then  $C = B$ .*

We also discuss the construction of minimal imitations of closed convex sets that show among other things that Theorem 1 is sharp. (Received September 17, 2010)