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Park Avenue, Florham Park, NJ 07932. *Changing Base without Losing Space.*

We describe a simple, but powerful local encoding technique, implying two surprising results:

**1.** We show how to represent a vector of  $n$  values from a set  $\Sigma$  using  $\lceil n \log_2 |\Sigma| \rceil$  bits, such that reading or writing any entry takes  $O(1)$  time. This demonstrates, for instance, an “equivalence” between decimal and binary computers, and has been a central toy problem in the field of succinct data structures. Previous solutions required space of  $n \log_2 |\Sigma| + n/\lg^{O(1)} n$  bits for constant access.

**2.** Given a stream of  $n$  bits arriving online (for any  $n$ , not known in advance), we can output a *prefix-free* encoding that uses  $n + \log_2 n + O(\lg \lg n)$  bits. The encoding and decoding algorithms only require  $O(\lg n)$  bits of memory, and run in constant time per word. This result is interesting in cryptographic applications, as prefix-free codes are the simplest counter-measure to extensions attacks on hash functions, message authentication codes and pseudorandom functions. Our result refutes a conjecture of [Maurer, Sjödin 2005] on the hardness of online prefix-free encodings. (Received September 20, 2010)